



# NAIC Scenario Set Technical Documentation

Corporate Yield Model

## Table of Contents

1	NAIC Basic Data Set .....	2
2	Corporate Yield Model.....	3
2.1	Corporate Bond Spread – Stylized Facts .....	3
2.2	Corporate Yield Model Specification.....	5
3	Calibration Criteria .....	6
4	Summary .....	7
5	Additional Reading .....	7
	Disclosures/Confidentiality Notice.....	10

## 1 NAIC Basic Data Set

The Basic Data Set provided free of charge to insurers is the standard scenario file set delivered as part of the NAIC scenario service. Users can access the scenarios online by downloading a file containing stochastic scenarios from the GEMS® Economic Scenario Generator (ESG) for real-world interest rates, equity and bond fund returns. The typical application for these scenarios is in calculations of life and annuity Statutory reserves according the Valuation Manual (e.g., VM-20, VM-21) and capital under the NAIC RBC requirements (e.g., C3 Phase 1, C3 Phase 2).

In this document the technical specification of the underlying stochastic model of the ESG used for producing corporate bond yields, spreads and returns on corporate bond funds for the Basic Data Set are described.

## 2 Corporate Yield Model

Corporate bonds have become an increasingly important asset class in the past decade. The drive into corporate debt has been driven in part by a sustained period of low yields. Scenarios for the yields and spreads on corporate bonds as well as corporate bond fund returns are simulated using a multi-factor model referred to as the Corporate Yield Model.

The model incorporates the following important features:

- Stochastic spreads
- Stochastic transition and default dynamics
- Real World and Risk Neutral versions
- Ability to produce the jump like behavior in spreads
- Mechanism for fitting the initial yield curves of corporate bonds across multiple ratings and tenors
- Pricing of bonds within an arbitrage free framework

### 2.1 Corporate Bond Spread – Stylized Facts

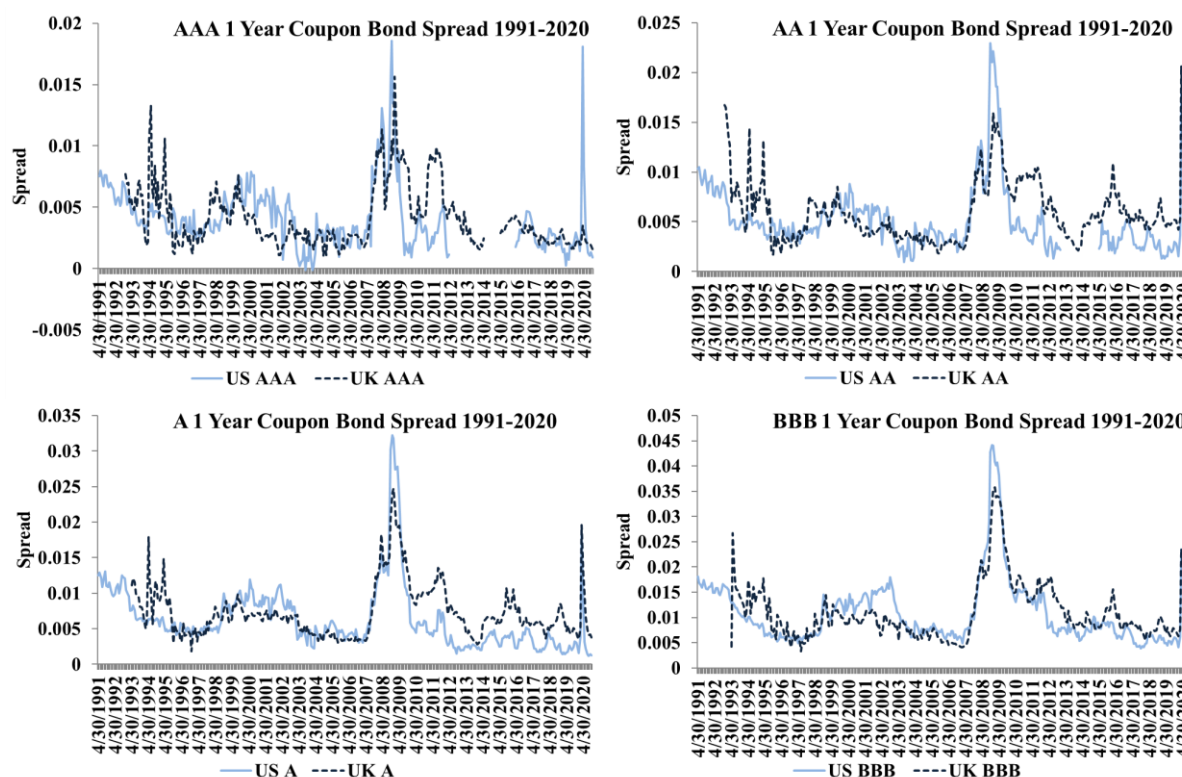


Figure 1 Spreads for US and UK AAA, AA, A and BBB rated bonds of 1-year maturity from 1991-2020, showing the sudden and rapid increases in spread experienced in 2008/2009 and early in 2020. (Source: Bloomberg/Conning)

The events of 2008 and several market events since were characterized by falling equity markets and increasing spreads on corporate bonds. Figure 1 shows the historical spreads on 1-year AAA, AA, A and BBB rated bonds from the United States and United Kingdom. While periods of high volatility had been observed before, the events of 2008 were unprecedented in

the albeit short historical record. During this period spreads increased rapidly in most cases to levels which were over twice the highest levels previously experienced, and between 4 and 5 times the historical mean. Figure 1 also supports the argument that corporate bond spreads are stochastic and capable of exhibiting dislocations similar, but evolving more slowly, than those observed in the equity markets.

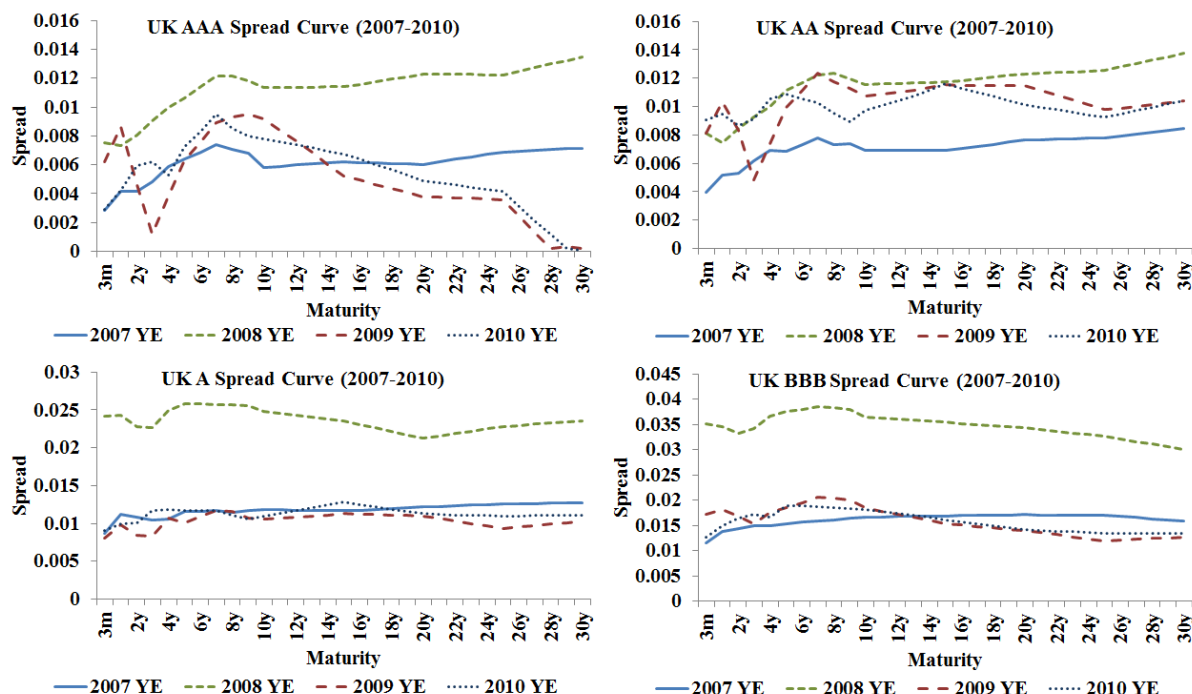


Figure 2 Spreads curves for UK AAA, AA, A and BBB rated bonds at year end 2007-2010, showing the extent of the difference between 2008 and other years. Also obvious is the extent to which market spread curves exhibit a range of shapes and are not smooth. (Source: Bloomberg/Conning)

Another important feature of the market is the correlation of credit spreads with other market sectors, in particular equities. Empirical evidence indicates that the lower the rating of a bond the more the bond behaves like an equity instrument. Consequently, one expects there to be an increasing correlation between corporate bond spreads and equity returns as ratings decline. This is indeed what is observed in the market data, in particular for lower credit ratings of corporate bonds.

Figure 2 shows the term structure of credit spreads for UK AAA, AA, A and BBB rated bonds at year end 2007, 2008, 2009 and 2010. Here again we can observe that the movement in spreads between 2007 and 2008 effected all ratings and tenors simultaneously. We also observe some possible liquidity effects in these curves, such as the AAA curve in 2009. Such discontinuities in the spread curves for some tenors require a special consideration, particularly in the context of fitting initial yield curves for the corporate bond markets.

This summarizes some of the main features of the market that a model of corporate bond yields and spreads would ideally exhibit.

## 2.2 Corporate Yield Model Specification

The GEMS Corporate Yield Model is a multifactor reduced form model allowing for the production and simulation of corporate bond yields, spreads, bond prices, transitions between rating classes and defaults. As a starting point for the model we assume that there are  $K$  rating classes  $\{1, 2, \dots, K-1, K\}$  where the absorbing state  $K$  is default. The rating classes used for the Basic Data Set are  $\{AAA, AA, A, BBB, HIGH\ YIELD, DEFAULT\}$ .

Two primary inputs govern the dynamics of the model.

- 1)  $K \times K$ -generator matrix,  $\mathcal{L}(t)$ , for the rating transition and default.
- 2) A stochastic modulator  $\mu(t)$  which multiplies the generator matrix  $\mathcal{L}(t)$  at each time step.

The form of the generator matrix  $\mathcal{L}(t)$  can be written as:

$$\mathcal{L}(t) = \begin{bmatrix} \lambda_{1,1}(t) & \lambda_{1,2}(t) & \lambda_{1,3}(t) & \cdots & \lambda_{1,K}(t) \\ \lambda_{2,1}(t) & \lambda_{2,2}(t) & \lambda_{2,3}(t) & \cdots & \lambda_{2,K}(t) \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \lambda_{K-1,1}(t) & \lambda_{K-1,2}(t) & \lambda_{K-1,3}(t) & \cdots & \lambda_{K-1,K}(t) \\ 0 & 0 & 0 & \cdots & 0 \end{bmatrix}$$

With the dynamics of the model governed by the stochastic generator:

$$\mathcal{L}(t)\mu(t)$$

The generator matrix is a transformation of the corporate bond transition matrix which everyone familiar with the corporate bond markets knows. The relationship between the real-world transition matrix  $Q^{RW}$  and the generator matrix is:

$$Q^{RW} = e^{\mathcal{L}(t)}$$

The properties of the generator matrix are that the rows sum to zero, the diagonal elements are negative, and the off-diagonal elements take positive values. The generator matrix has useful properties in the context of stochastic modeling. In particular a generator matrix multiplied by a scalar, such as  $\mu(t)$  is still a generator matrix. The same is not true of a transition matrix because the rows sum to 1.

In addition to the above the model incorporates the following characteristics.

- 1) A recovery of market value assumption for each rating class, defining the proportion of a bond's price prior to default that is recovered on default.
- 2) A mechanism for fitting the initial yield curves of corporate bonds for different ratings and tenor.
- 3) A jump process as one element of the stochastic modulator  $\mu(t)$  allowing for the simulation of rapid increases in corporate bond spreads.
- 4) A correlation between the stochastic modulator  $\mu(t)$  and the model of equity returns.

Figure 3 shows the GEMS simulated 1-year maturity spread for AAA, AA, A, BBB and High Yield bonds over a 30 year simulation horizon in quarterly time steps. The spread jump is clearly visible in this path, and as with real credit crises the shock is systemic, affecting assets of all ratings simultaneously. Models which do not incorporate such a jump process have difficulty in producing these levels of spreads without large increases in the overall volatility of spreads to unrealistic levels.

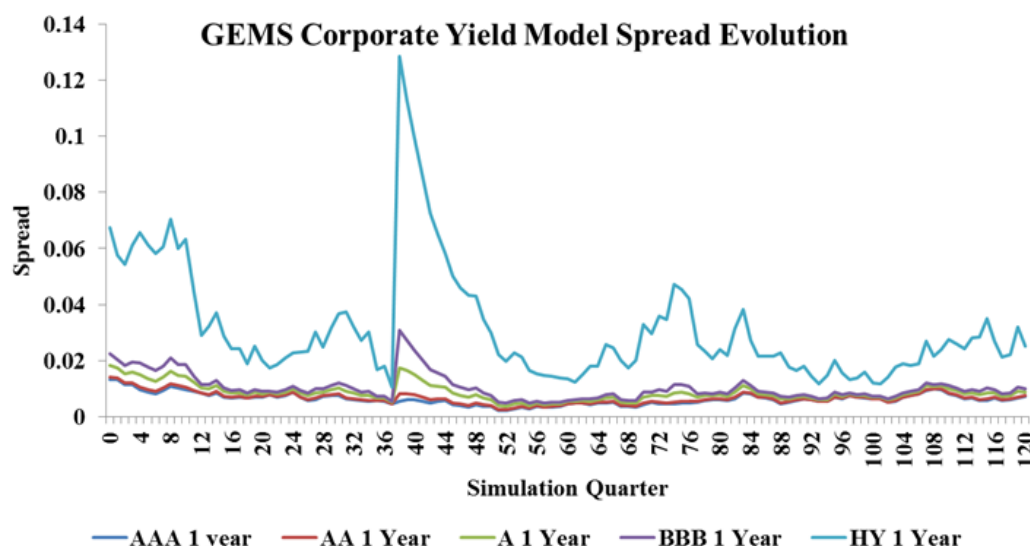


Figure 3 Simulated path from the GEMS Corporate Yield Model showing spreads on bonds of 1 year maturity for AAA, AA, A, BBB and High Yield rating classes. (source: Conning GEMS® ESG)

This jump process leads to bond returns which are fat tailed, capturing the types of extreme losses that can occur through spread movements as well as defaults. Figure 4 shows a Q-Q plot

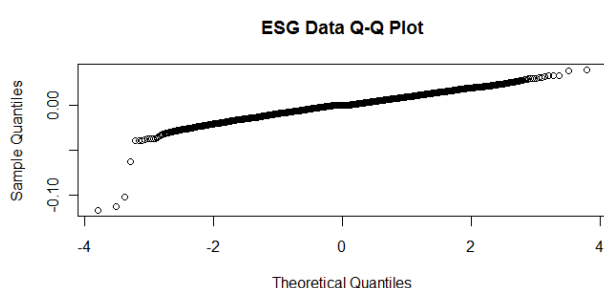


Figure 4 Q-Q Plot of A rated 3-5 year corporate bond returns. (Source: Conning GEMS® ESG).

for A rated bond returns with maturity 3 to 5 years based on the output from the corporate yield model. If the returns were normally distributed, then the Q-Q plot would show a straight line. However, the left tail of the plot is observed to deviate significantly from a straight line, indicating a significantly heavy loss tail in the return distribution of the model.

### 3 Calibration Criteria

The calibration criteria for the models consists of a set of target values for the distributional properties of nominal interest rates at future time horizons. The precise methodology and final

calibration targets are currently under discussion. More information will be added to this section when the details are known.

## 4 Summary

In this document the technical specification and the properties of the corporate spread and corporate bond fund returns model used to produce the NAIC Basic Data Set have been described. The GEMS® corporate yield model described represents an advanced modeling structure for this asset class which enables more realistic modeling of real world effects than is possible with a simpler model. Prior to scenario production the model is approximately fit to the initial market yield curve of corporate bonds across the five modelled rating categories for maturities 1 to 10 years. The statistical properties of the simulated model can also be customized to take account of specified or changing calibration criteria.

## 5 Additional Reading

Duffie and Singleton, *Modeling Term Structures of Defaultable Bonds*, The Review of Financial Studies, 1999.

Lando, D. (2004). *Credit Risk modeling*. Princeton University Press

## 6 Appendices

### 6.1 Appendix I – Relevant Tickers

The following tickers may be relevant as validation benchmarks for the stochastic output of the GEMS® interest rate model. Conning does not supply, distribute or directly derive the models from this data and is supplied here for guidance only.

Description	Ticker
AAA Industrial Coupon Yield, 3 month	BVCVPO3M Index
AAA Industrial Coupon Yield, 6 month	BVCVPO6M Index
AAA Industrial Coupon Yield, 1 year	BVCVPO01 Index
AAA Industrial Coupon Yield, 2 year	BVCVPO02 Index
AAA Industrial Coupon Yield, 3 year	BVCVPO03 Index
AAA Industrial Coupon Yield, 4 year	BVCVPO04 Index
AAA Industrial Coupon Yield, 5 year	BVCVPO05 Index
AAA Industrial Coupon Yield, 7 year	BVCVPO07 Index
AAA Industrial Coupon Yield, 8 year	BVCVPO08 Index
AAA Industrial Coupon Yield, 9 year	BVCVPO09 Index
AAA Industrial Coupon Yield, 10 year	BVCVPO10 Index
AAA Industrial Coupon Yield, 15 year	BVCVPO15 Index
AAA Industrial Coupon Yield, 20 year	BVCVPO20 Index
AAA Industrial Coupon Yield, 25 year	BVCVPO25 Index



AAA Industrial Coupon Yield, 30 year	BVCVPO30 Index
AA Industrial Yield, 3 month	IGUUID3M Index
AA Industrial Yield, 6 month	IGUUID6M Index
AA Industrial Yield, 1 year	IGUUID01 Index
AA Industrial Yield, 2 year	IGUUID02 Index
AA Industrial Yield, 3 year	IGUUID03 Index
AA Industrial Yield, 4 year	IGUUID04 Index
AA Industrial Yield, 5 year	IGUUID05 Index
AA Industrial Yield, 7 year	IGUUID07 Index
AA Industrial Yield, 8 year	IGUUID08 Index
AA Industrial Yield, 9 year	IGUUID09 Index
AA Industrial Yield, 10 year	IGUUID10 Index
AA Industrial Yield, 15 year	IGUUID15 Index
AA Industrial Yield, 20 year	IGUUID20 Index
AA Industrial Yield, 25 year	IGUUID25 Index
AA Industrial Yield, 30 year	IGUUID30 Index
A Industrial Yield, 3 month	BVCSUP3M Index
A Industrial Yield, 6 month	BVCSUP6M Index
A Industrial Yield, 1 year	BVCSUP1 Index
A Industrial Yield, 2 year	BVCSUP2 Index
A Industrial Yield, 3 year	BVCSUP3 Index
A Industrial Yield, 4 year	BVCSUP4 Index
A Industrial Yield, 5 year	BVCSUP5 Index
A Industrial Yield, 7 year	BVCSUP7 Index
A Industrial Yield, 8 year	BVCSUP8 Index
A Industrial Yield, 9 year	BVCSUP9 Index
A Industrial Yield, 10 year	BVCSUP10 Index
A Industrial Yield, 15 year	BVCSUP15 Index
A Industrial Yield, 20 year	BVCSUP20 Index
A Industrial Yield, 25 year	BVCSUP25 Index
A Industrial Yield, 30 year	BVCSUP30 Index
BBB Industrial Yield, 3 month	IGUUAD3M Index
BBB Industrial Yield, 6 month	IGUUAD6M Index
BBB Industrial Yield, 1 year	IGUUAD01 Index
BBB Industrial Yield, 2 year	IGUUAD02 Index
BBB Industrial Yield, 3 year	IGUUAD03 Index
BBB Industrial Yield, 4 year	IGUUAD04 Index
BBB Industrial Yield, 5 year	IGUUAD05 Index
BBB Industrial Yield, 7 year	IGUUAD07 Index
BBB Industrial Yield, 8 year	IGUUAD08 Index
BBB Industrial Yield, 9 year	IGUUAD09 Index
BBB Industrial Yield, 10 year	IGUUAD10 Index
BBB Industrial Yield, 15 year	IGUUAD15 Index
BBB Industrial Yield, 20 year	IGUUAD20 Index
BBB Industrial Yield, 25 year	IGUUAD25 Index
BBB Industrial Yield, 30 year	IGUUAD30 Index
BB Industrial Yield, 3 month	IGUUI53M Index



BB Industrial Yield, 6 month	IGUUI56M Index
BB Industrial Yield, 1 year	IGUUI501 Index
BB Industrial Yield, 2 year	IGUUI502 Index
BB Industrial Yield, 3 year	IGUUI503 Index
BB Industrial Yield, 4 year	IGUUI504 Index
BB Industrial Yield, 5 year	IGUUI505 Index
BB Industrial Yield, 7 year	IGUUI507 Index
BB Industrial Yield, 8 year	IGUUI508 Index
BB Industrial Yield, 9 year	IGUUI509 Index
BB Industrial Yield, 10 year	IGUUI510 Index
BB Industrial Yield, 15 year	IGUUI515 Index
BB Industrial Yield, 20 year	IGUUI520 Index
BB Industrial Yield, 25 year	IGUUI525 Index
BB Industrial Yield, 30 year	IGUUI530 Index

## Disclosures/Confidentiality Notice

Conning ([www.conning.com](http://www.conning.com)) is a leading investment management firm with a long history of serving the insurance industry. Conning supports institutional investors, including pension plans, with investment solutions and asset management offerings, award-winning risk modeling software, and industry research. Founded in 1912, Conning has investment centers in Asia, Europe and North America.

© Conning, Inc. This document and the software described therein are copyrighted with all rights reserved by Conning, Inc. (“Conning”). This document is intended only to inform readers about general developments of interest and does not constitute investment advice. The information contained herein is not guaranteed to be complete or accurate and Conning cannot be held liable for any errors in or any reliance upon this information. Any opinions contained herein are subject to change at any time without notice.

This document contains information that is confidential or proprietary to Conning and is provided solely for the benefit of the Conning client authorized to download the document, including those affiliates permitted under the applicable Software License Agreement. The document may be used for the client's internal use and for independent reviews by the client's auditors and regulatory bodies (“Permitted Third Parties”). Conning must, however, be notified in advance of all Permitted Third Parties to which the client intends to distribute the document and the purpose for such distribution. By accepting this document you agree that: (1) if there is any pre-existing contract containing disclosure and use restrictions between you and/or your company and Conning you and your company will use this information in reliance on and subject to the terms of any such pre-existing contract, as permitted by this notice or as may be required by law; or (2) if there is no contractual relationship between you and/or your company and Conning, you and your company agree to protect this information and not to reproduce, disclose or use the information in any way, except as may be required by law or as permitted by this notice. Except as set forth in this notice, no part of this document may be distributed by any means or used for any purpose except with Conning’s prior written authorization. Any third parties that are given access to the document are subject to the same the terms of this notice. Any distribution of this document, in whole or in party, must always include this notice.

ADVISE®, FIRM®, and GEMS® are registered trademarks of Conning, Inc. Copyright Conning, Inc. All rights reserved. ADVISE®, FIRM®, and GEMS® are proprietary software published and owned by Conning, Inc.